

# Demonstration of the Iris separation logic in Coq

Robbert Krebbers<sup>1</sup>

Delft University of Technology, The Netherlands

January 21, 2017 @ Coq PL, Paris, France

---

<sup>1</sup>Iris is joint work with: Ralf Jung, Jacques-Hendri Jourdan, Aleš Bizjak, David Swasey, Filip Sieczkowski, Kasper Svendsen, Aaron Turon, Amin Timany, Derek Dreyer, and Lars Birkedal

## Iris Proof Mode (IPM)

**Goal:** reasoning in an object logic in the same style as reasoning in Coq

## Iris Proof Mode (IPM)

**Goal:** reasoning in an object logic in the same style as reasoning in Coq

# Iris Proof Mode (IPM)

**Goal:** reasoning in an object logic in the same style as reasoning in Coq

**How?**

- ▶ Extend Coq with (spatial and non-spatial) named proof contexts for an object logic
- ▶ Tactics for introduction and elimination of all connectives of the object logic
- ▶ Entirely implemented using reflection, type classes and Ltac (no OCaml plugin needed)

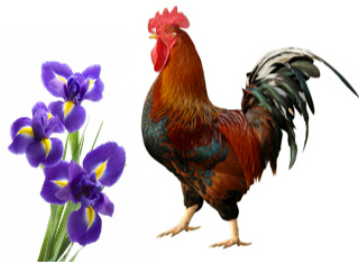


# Iris Proof Mode (IPM)

**Goal:** reasoning in **Iris** in the same style as reasoning in Coq

**How?**

- ▶ Extend Coq with (spatial and non-spatial) named proof contexts for **Iris**
- ▶ Tactics for introduction and elimination of all connectives of **Iris**
- ▶ Entirely implemented using reflection, type classes and Ltac (no OCaml plugin needed)



**Iris:** language independent higher-order separation logic for modular reasoning about fine-grained concurrency in Coq

# Demo



## The setup of IPM in a nutshell

- ▶ Deep embedding of contexts as association lists:

```
Record envs :=  
  Envs { env_persistent : env iProp; env_spatial : env iProp }.  
Coercion of_envs ( $\Delta$  : envs) : iProp :=  
  (  $\ulcorner$  envs_wf  $\Delta$   $\urcorner$  *  $\square$  [*] env_persistent  $\Delta$  * [*] env_spatial  $\Delta$  )%I.
```

## The setup of IPM in a nutshell

- ▶ Deep embedding of contexts as association lists:

```
Record envs :=  
  Envs { env_persistent : env iProp; env_spatial : env iProp }.  
Coercion of envs (Δ : envs) : iProp :=  
  (⌈ envs_wf Δ ⌈ * □ [*] env_persistent Δ * [*] env_spatial Δ ⌋)ᵒᵃ.
```

Propositions that enjoy  $P \Leftrightarrow P * P$



# The setup of IPM in a nutshell

- ▶ Deep embedding of contexts as association lists:

```
Record envs :=  
  Envs { env_persistent : env iProp; env_spatial : env iProp }.  
Coercion of_envs (Δ : envs) : iProp :=  
  (⌈ envs_wf Δ ⌋ * □ [*] env_persistent Δ * [*] env_spatial Δ)%I.
```

Propositions that enjoy  $P \Leftrightarrow P * P$

- ▶ Tactics implemented by reflection:

```
Lemma tac_sep_split Δ Δ1 Δ2 lr js Q1 Q2 :  
  envs_split lr js Δ = Some (Δ1, Δ2) →  
  (Δ1 ⊢ Q1) → (Δ2 ⊢ Q2) → Δ ⊢ Q1 * Q2.
```

# The setup of IPM in a nutshell

- ▶ Deep embedding of contexts as association lists:

```
Record envs :=  
  Envs { env_persistent : env iProp; env_spatial : env iProp }.  
Coercion of_envs (Δ : envs) : iProp :=  
  (⌈ envs_wf Δ ⌋ * □ [*] env_persistent Δ * [*] env_spatial Δ)%I.
```

Propositions that enjoy  $P \Leftrightarrow P * P$

- ▶ Tactics implemented by reflection:

```
Lemma tac_sep_split Δ Δ1 Δ2 lr js Q1 Q2 :  
  envs_split lr js Δ = Some (Δ1, Δ2) →  
  (Δ1 ⊢ Q1) → (Δ2 ⊢ Q2) → Δ ⊢ Q1 * Q2.
```

Context splitting implemented in Gallina

# The setup of IPM in a nutshell

- ▶ Deep embedding of contexts as association lists:

```
Record envs :=  
  Envs { env_persistent : env iProp; env_spatial : env iProp }.  
Coercion of envs (Δ : envs) : iProp :=  
  (⌈ envs_wf Δ ⌉ * □ [*] env_persistent Δ * [*] env_spatial Δ)%aI.
```

Propositions that enjoy  $P \Leftrightarrow P * P$

- ▶ Tactics implemented by reflection:

```
Lemma tac_sep_split Δ Δ1 Δ2 lr js Q1 Q2 :  
  envs_split lr js Δ = Some (Δ1, Δ2) →  
  (Δ1 ⊢ Q1) → (Δ2 ⊢ Q2) → Δ ⊢ Q1 * Q2.
```

Context splitting implemented in Gallina

- ▶ Ltac wrappers around reflective tactics:

```
Tactic Notation "iSplitL" constr(Hs) :=  
  let Hs := words Hs in  
  eapply tac_sep_split with _ _ false Hs _ _;  
  [env_cbv; reflexivity || fail "iSplitL: hypotheses" Hs "not found in the context"  
  | (* goal 1 *) | (* goal 2 *) ].
```

Report sensible error to the user

# This talk

Demonstrate some uses of IPM:

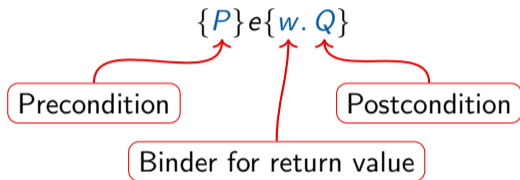
- ▶ Symbolic execution
- ▶ Lock based concurrency
- ▶ Verification of a spin lock



## Part #1: symbolic execution

# Hoare triples

**Hoare triples** for partial program correctness:



If the initial state satisfies  $P$ , then:

- ▶  $e$  does not get stuck/crash
- ▶ if  $e$  terminates with value  $v$ , the final state satisfies  $Q[v/w]$

## Separation logic [O'Hearn, Reynolds, Yang]

### The points-to connective $x \mapsto v$

- ▶ provides the knowledge that location  $x$  has value  $v$ , and
- ▶ provides **exclusive ownership** of  $x$

### Separating conjunction $P * Q$ :

the state consists of *disjoint parts* satisfying  $P$  and  $Q$

## Separation logic [O'Hearn, Reynolds, Yang]

**The points-to connective**  $x \mapsto v$

- ▶ provides the knowledge that location  $x$  has value  $v$ , and
- ▶ provides **exclusive ownership** of  $x$

**Separating conjunction**  $P * Q$ :

the state consists of *disjoint parts* satisfying  $P$  and  $Q$

Example:

$\{x \mapsto v_1 * y \mapsto v_2\} \text{swap}(x, y) \{w. w = () \wedge x \mapsto v_2 * y \mapsto v_1\}$

the  $*$  ensures that  $x$  and  $y$  are different



## Proving Hoare triples using IPM

Consider:

$$\{x \mapsto v_1 * y \mapsto v_2\} \text{swap}(x, y) \{x \mapsto v_2 * y \mapsto v_1\}$$

How to use IPM to manipulate the precondition?

# Proving Hoare triples using IPM

Consider:

$$\{x \mapsto v_1 * y \mapsto v_2\} \text{swap}(x, y) \{x \mapsto v_2 * y \mapsto v_1\}$$

How to use IPM to manipulate the precondition?

**Solution: define Hoare triple in terms of weakest preconditions**

We let:

$$\{P\} e \{w. Q\} \triangleq \square(P \text{ -* wp } e \{w. Q\})$$

where  $\text{wp } e \{w. Q\}$  gives the *weakest precondition* under which:

- ▶ all executions of  $e$  are safe
- ▶ if  $e$  terminates with value  $v$ , the final state satisfies  $Q[v/w]$

## Rules for weakest precondition

Rule of 'consequence':

$$\text{wp } e \{v. \text{wp } K[v] \{\Phi\}\} \quad \multimap \quad \text{wp } K[e] \{\Phi\}$$

Value rule:

$$\Phi v \quad \multimap \quad \text{wp } v \{\Phi\}$$

Lambda rule:

$$\text{wp } e[v/x] \{\Phi\} \quad \multimap \quad \text{wp } (\lambda x. e)v \{\Phi\}$$

## Stateful rules for weakest preconditions

Let us just translate the Hoare rules naively:

$$\begin{aligned}l \mapsto v & \quad \text{---} * \quad \text{wp } !l \{w. w = v * l \mapsto v\} \\l \mapsto v_1 & \quad \text{---} * \quad \text{wp } l := v_2 \{w. w = () * l \mapsto v_2\}\end{aligned}$$

Problems:

- ▶ Having to frame and weaken to apply these rules
- ▶ Equalities in the postconditions

## Stateful rules for weakest preconditions

Let us just translate the Hoare rules naively:

$$\begin{aligned} l \mapsto v & \quad * \quad \text{wp } !l \{w. w = v * l \mapsto v\} \\ l \mapsto v_1 & \quad * \quad \text{wp } l := v_2 \{w. w = () * l \mapsto v_2\} \end{aligned}$$

Problems:

- ▶ Having to frame and weaken to apply these rules
- ▶ Equalities in the postconditions

'Backwards' or 'predicate transformer' formulation:

$$\begin{aligned} l \mapsto v & \quad * \quad (l \mapsto v \text{ } * \text{ } \Phi v) \quad * \quad \text{wp } !l \{\Phi\} \\ l \mapsto v_1 & \quad * \quad (l \mapsto v_2 \text{ } * \text{ } \Phi ()) \quad * \quad \text{wp } l := v_2 \{\Phi\} \end{aligned}$$

Resources that have to be given up

Resources that are given back

## Nicer definition of the Hoare triple [J-O. Kaiser]

$$\{P\} e \{ \vec{x} \text{RET } w. Q \} \triangleq \Box (\forall \Phi. P \multimap (\forall \vec{x}. Q \multimap \Phi w) \multimap \text{wp } e \{ \Phi \})$$

Resources that have to be given up

Resources that are given back

# Demo



## **Part #2:** lock based concurrency



## Concurrent separation logic [O'Hearn]

The *par* rule:

$$\frac{\{P_1\} e_1 \{Q_1\} \quad \{P_2\} e_2 \{Q_2\}}{\{P_1 * P_2\} e_1 || e_2 \{Q_1 * Q_2\}}$$

## Concurrent separation logic [O'Hearn]

The *par* rule:

$$\frac{\{P_1\}e_1\{Q_1\} \quad \{P_2\}e_2\{Q_2\}}{\{P_1 * P_2\}e_1 || e_2\{Q_1 * Q_2\}}$$

For example:

$$\begin{array}{c} \{x \mapsto 4 * y \mapsto 6\} \\ \parallel \\ x := !x + 2 \quad \parallel \quad y := !y + 2 \\ \parallel \\ \{x \mapsto 6 * y \mapsto 8\} \end{array}$$

## Concurrent separation logic [O'Hearn]

The *par* rule:

$$\frac{\{P_1\}e_1\{Q_1\} \quad \{P_2\}e_2\{Q_2\}}{\{P_1 * P_2\}e_1 || e_2\{Q_1 * Q_2\}}$$

For example:

$$\frac{\begin{array}{c} \{x \mapsto 4 * y \mapsto 6\} \\ \{x \mapsto 4\} \quad \parallel \quad \{y \mapsto 6\} \\ x := !x + 2 \quad \parallel \quad y := !y + 2 \end{array}}{\{x \mapsto 6 * y \mapsto 8\}}$$

## Concurrent separation logic [O'Hearn]

The *par* rule:

$$\frac{\{P_1\}e_1\{Q_1\} \quad \{P_2\}e_2\{Q_2\}}{\{P_1 * P_2\}e_1 || e_2\{Q_1 * Q_2\}}$$

For example:

$$\begin{array}{c} \{x \mapsto 4 * y \mapsto 6\} \\ \{x \mapsto 4\} \quad || \quad \{y \mapsto 6\} \\ x := !x + 2 \quad || \quad y := !y + 2 \\ \{x \mapsto 6\} \quad || \quad \{y \mapsto 8\} \\ \{x \mapsto 6 * y \mapsto 8\} \end{array}$$

## Concurrent separation logic [O'Hearn]

The *par* rule:

$$\frac{\{P_1\} e_1 \{Q_1\} \quad \{P_2\} e_2 \{Q_2\}}{\{P_1 * P_2\} e_1 || e_2 \{Q_1 * Q_2\}}$$

For example:

$$\begin{array}{c} \{x \mapsto 4 * y \mapsto 6\} \\ \{x \mapsto 4\} \quad || \quad \{y \mapsto 6\} \\ x := !x + 2 \quad || \quad y := !y + 2 \\ \{x \mapsto 6\} \quad || \quad \{y \mapsto 8\} \\ \{x \mapsto 6 * y \mapsto 8\} \end{array}$$

Works great for concurrent programs without shared memory: concurrent quick sort, concurrent merge sort, ...

## What about shared state?

A simple problem:

```
{True}  
let x = ref(0) in  
let y = ref(4) in
```

```
swap x y || assert (!x + !y = 4)
```

```
{True}
```

## What about shared state?

A simple problem:

```
{True}
let x = ref(0) in
let y = ref(4) in
let z = new_lock() in
acquire z || acquire z
swap x y  || assert (!x + !y = 4)
release z || release z
{True}
```

# Specification of a lock

Specifications of the operations:

Lock invariant

↓

$$\begin{array}{l} \{P\} \text{new\_lock}() \{I. \text{IsLock}(I, P)\} \\ \{\text{IsLock}(I, P)\} \text{acquire } I \{P\} \\ \{\text{IsLock}(I, P) * P\} \text{release } I \{\text{True}\} \end{array}$$

The `IsLock` predicate can be shared among threads:

$$\text{IsLock}(I, P) \Leftrightarrow \text{IsLock}(I, P) * \text{IsLock}(I, P)$$



# Specification of a lock

Specifications of the operations:

Lock invariant



$\{P\} \text{new\_lock()} \{I. \text{IsLock}(I, P)\}$

$\{\text{IsLock}(I, P)\} \text{acquire } I \{P * \text{Locked}(I)\}$

$\{\text{IsLock}(I, P) * \text{Locked}(I) * P\} \text{release } I \{\text{True}\}$

The `IsLock` predicate can be shared among threads:

$\text{IsLock}(I, P) \Leftrightarrow \text{IsLock}(I, P) * \text{IsLock}(I, P)$

## The proof of our program

{True}

let  $x = \text{ref}(0)$  in

let  $y = \text{ref}(4)$  in

let  $z = \text{new\_lock}()$  in

*acquire*  $z$

*swap*  $x\ y$

*release*  $z$

{True}

*acquire*  $z$

**assert** ( $!x + !y = 4$ )

*release*  $z$

## The proof of our program

```
{True}  
let x = ref(0) in  
{x ↦ 0}  
let y = ref(4) in  
  
let z = new_lock() in
```

*acquire z*

*swap x y*

*release z*

```
{True}
```

*acquire z*

**assert** (!x + !y = 4)

*release z*

## The proof of our program

```
{True}  
let x = ref(0) in  
{x ↦ 0}  
let y = ref(4) in  
{x ↦ 0 * y ↦ 4}  
let z = new_lock() in
```

*acquire z*

*swap x y*

*release z*

```
{True}
```

*acquire z*

**assert** (!x + !y = 4)

*release z*

## The proof of our program

```
{True}
let x = ref(0) in
{x ↦ 0}
let y = ref(4) in
{x ↦ 0 * y ↦ 4}
let z = new_lock() in
allocate lsLock(z, ∃n1, n2. x ↦ n1 * y ↦ n2 * n1 + n2 = 4)

acquire z
swap x y
release z

{True}
```

||

```
acquire z
assert (!x + !y = 4)
release z
```

# The proof of our program

```
{True}
let x = ref(0) in
{x ↦ 0}
let y = ref(4) in
{x ↦ 0 * y ↦ 4}
let z = new_lock() in
allocate lsLock(z, ∃n1, n2. x ↦ n1 * y ↦ n2 * n1 + n2 = 4)
{True}
acquire z

swap x y

release z

{True}
```

||

```
{True}
acquire z

assert (!x + !y = 4)

release z
```

## The proof of our program

```
{True}
let x = ref(0) in
{x ↦ 0}
let y = ref(4) in
{x ↦ 0 * y ↦ 4}
let z = new_lock() in
allocate lsLock(z, ∃n1, n2. x ↦ n1 * y ↦ n2 * n1 + n2 = 4)
{True}
acquire z
{x ↦ n1 * y ↦ n2 * n1 + n2 = 4}
swap x y

release z

{True}
```

	{True}
	acquire z
	assert (!x + !y = 4)
	release z

## The proof of our program

```
{True}
let x = ref(0) in
{x ↦ 0}
let y = ref(4) in
{x ↦ 0 * y ↦ 4}
let z = new_lock() in
allocate lsLock(z, ∃n1, n2. x ↦ n1 * y ↦ n2 * n1 + n2 = 4)
{True}
acquire z
{x ↦ n1 * y ↦ n2 * n1 + n2 = 4}
swap x y
{x ↦ n2 * y ↦ n1 * n1 + n2 = 4}
release z

{True}
||
{True}
acquire z
assert (!x + !y = 4)
release z
```



## The proof of our program

```
{True}
let x = ref(0) in
{x ↦ 0}
let y = ref(4) in
{x ↦ 0 * y ↦ 4}
let z = new_lock() in
allocate lsLock(z, ∃n1, n2. x ↦ n1 * y ↦ n2 * n1 + n2 = 4)
{True}
acquire z
{x ↦ n1 * y ↦ n2 * n1 + n2 = 4}
swap x y
{x ↦ n2 * y ↦ n1 * n1 + n2 = 4}
release z
{True}
{True}
```

{True}	acquire z
assert (!x + !y = 4)	
release z	

## The proof of our program

```
{True}
let x = ref(0) in
{x ↦ 0}
let y = ref(4) in
{x ↦ 0 * y ↦ 4}
let z = new_lock() in
allocate lsLock(z, ∃n1, n2. x ↦ n1 * y ↦ n2 * n1 + n2 = 4)
{True}
acquire z
{x ↦ n1 * y ↦ n2 * n1 + n2 = 4}
swap x y
{x ↦ n2 * y ↦ n1 * n1 + n2 = 4}
release z
{True}
{True}
```

	{True}
	acquire z
	{x ↦ n <sub>1</sub> * y ↦ n <sub>2</sub> * n <sub>1</sub> + n <sub>2</sub> = 4}
	assert (!x + !y = 4)
	release z

## The proof of our program

```
{True}
let x = ref(0) in
{x ↦ 0}
let y = ref(4) in
{x ↦ 0 * y ↦ 4}
let z = new_lock() in
allocate lsLock(z, ∃n1, n2. x ↦ n1 * y ↦ n2 * n1 + n2 = 4)
{True}
acquire z
{x ↦ n1 * y ↦ n2 * n1 + n2 = 4}
swap x y
{x ↦ n2 * y ↦ n1 * n1 + n2 = 4}
release z
{True}
{True}
```

```
{True}
acquire z
{x ↦ n1 * y ↦ n2 * n1 + n2 = 4}
assert (!x + !y = 4)
{x ↦ n1 * y ↦ n2 * n1 + n2 = 4}
release z
```

## The proof of our program

```
{True}
let x = ref(0) in
{x ↦ 0}
let y = ref(4) in
{x ↦ 0 * y ↦ 4}
let z = new_lock() in
allocate lsLock(z, ∃n1, n2. x ↦ n1 * y ↦ n2 * n1 + n2 = 4)
{True}
acquire z
{x ↦ n1 * y ↦ n2 * n1 + n2 = 4}
swap x y
{x ↦ n2 * y ↦ n1 * n1 + n2 = 4}
release z
{True}
{True}
```

	{True}
	acquire z
	{x ↦ n <sub>1</sub> * y ↦ n <sub>2</sub> * n <sub>1</sub> + n <sub>2</sub> = 4}
	assert (!x + !y = 4)
	{x ↦ n <sub>1</sub> * y ↦ n <sub>2</sub> * n <sub>1</sub> + n <sub>2</sub> = 4}
	release z
	{True}

# Demo



## Part #3: verification of a spin lock

# Demo



## Part #4: conclusions



## Current Iris projects

- ▶ **Concurrent algorithms** (Jung, Krebbers, Swasey, Timany)
- ▶ **The Rust type system** (Jung, Jourdan, Dreyer, Krebbers)
- ▶ **Logical relations** (Krogh-Jespersen, Svendsen, Timany, Birkedal, Tassarotti, Jung, Krebbers)
- ▶ **Weak memory concurrency** (Kaiser, Dang, Dreyer, Lahav, Vafeiadis)
- ▶ **Object calculi** (Swasey, Dreyer, Garg)
- ▶ **Logical atomicity** (Krogh-Jespersen, Zhang, Jung)
- ▶ **Defining Iris in Iris** (Krebbers, Jung, Jourdan, Bizjak, Dreyer, Birkedal)

## Coq wish list

- ▶ Data types in Ltac
- ▶ Side-effecting tactics that can return a value
- ▶ More expressive parsing mechanism for tactic notations
- ▶ Exception handling in Ltac to generate better error messages
- ▶ Opt-out from backtracking Ltac semantics
- ▶ Better ways to seal-off definitions



Thank you!

Download Iris at <http://iris-project.org/>